

Design Criteria:

$$\begin{array}{llll} S_s := 1.25 & S_1 := 0.5 & S_{DS} := 0.83 & S_{D1} := 0.42 \\ R := 3.0 & I := 1.0 & T := 2.37 & T_L := 6 \end{array}$$

Calculate Approximate Period:

Height of building: $h_n := 20$

Table 12.8-2 parameters: $C_t := 0.02$ $x := 0.75$

Approximate Fundamental Period (12.8-7): $T_a := C_t \cdot h_n^x = 0.189$

Upper Limit Coefficient (Table 12.8-1): $C_u := 1.4$

Design Period (12.8.2):

$$T_d := \min(T, T_a \cdot C_u) = 0.265$$

Static Base Shear Coefficient (12.8.1.1):

$$C_s := \frac{S_{DS}}{\frac{R}{I}} = 0.277$$

$$C_{s_max} := \frac{S_{D1}}{T_d \cdot \frac{R}{I}} = 0.529$$

$$C_{s_min} := \text{if} \left(S_1 \geq 0.6, \frac{0.5 \cdot S_1}{\frac{R}{I}}, 0.01 \right) = 0.01$$

$$C_s := \min(C_{s_max}, \max(C_s, C_{s_min})) = 0.277$$

Seismic Mass:

$$W := 108.864 \text{ kip}$$

Static Base Shear (12.8.1):

$$V := C_s \cdot W = 30.119 \text{ kip}$$

Scaling Factors:

$$SF_{\min} := \frac{1}{\frac{R}{I}} = 0.333 \quad \text{ASCE 7-05 section 12.9.2}$$

$$V_{\text{dynamic_X}} := 21.862 \text{ kip} \quad \text{Taken from unscaled dynamic analysis X Axis}$$

$$V_{\text{dynamic_Y}} := 21.665 \text{ kip} \quad \text{Taken from unscaled dynamic analysis Y Axis}$$

$$SF_X := \max \left(SF_{\min}, \text{if} \left(V_{\text{dynamic_X}} < 0.85 \cdot V, \frac{0.85 \cdot V}{V_{\text{dynamic_X}}}, \frac{V}{V_{\text{dynamic_X}}} \right) \right) = 1.171$$

$$SF_Y := \max \left(SF_{\min}, \text{if} \left(V_{\text{dynamic_Y}} < 0.85 \cdot V, \frac{0.85 \cdot V}{V_{\text{dynamic_Y}}}, \frac{V}{V_{\text{dynamic_Y}}} \right) \right) = 1.182$$

Verification:

$$\text{Scaling Factor: } \frac{V}{V_{\text{dynamic_X}}} = 1.378$$

$$\text{Minimum Scaling Factor per (12.9.4): } 0.85 \cdot \frac{V}{V_{\text{dynamic_X}}} = 1.171$$

$$\text{Dynamic Base shear: } V_{\text{dynamic_X}} = 21.862 \text{ kip}$$

$$\text{Minimum Allowable Base Shear if dynamic } V \text{ is less than static: } 0.85 \cdot V = 25.601 \text{ kip}$$

$$\text{Base shear with Scaling Factor Applied: } V_{\text{dynamic_X}} \cdot SF_X = 25.601 \text{ kip}$$